

## Luvion Technical Summary Luvion Technical Summary

### Scope

### Scope

This document summarizes the repository implementation of the Luvion 22-of-33 threshold signature path.

The implementation is a two-round threshold signing system over the ML-DSA-65 parameter set. It supports:

33 total signer nodes.

22 required signer nodes per signing committee.

Shamir-shared secret material for

s1

,

s2

, and

t0

.

Persistent TCP signer nodes.

A

cluster\_sign

coordinator that probes nodes, selects a committee, runs the signing ceremony, aggregates partial responses, and verifies successful signatures.

The current

gen\_shares

path is a synthetic dealer for test and demo material. It is not production DKG.

Key Files

Key Files

File

File

Responsibility

Responsibility

src/params.rs

ML-DSA-65 constants and Luvion threshold constants.

src/signing.rs

Core 22-of-33 signing math: round 1, challenge, round 2, aggregation, verification.

src/shamir.rs

Shamir sharing and reconstruction helpers for polynomial vectors.

src/share\_io.rs

On-disk public key and node share formats.

src/wire.rs

Versioned frame protocol and DTOs shared by coordinator and nodes.

src/bin/gen\_shares.rs

Synthetic dealer that creates

pk.bin

and 33 node share files.

src/bin/node.rs

Persistent signer node process.

src/bin/cluster\_sign.rs

TCP cluster coordinator and CLI.

src/bin/\_cluster/mod.rs

Shared cluster driver logic for probing and ceremony execution.

tests/cluster\_sign\_tcp.rs

Persistent TCP cluster integration tests.

tests/coordinator\_integration.rs

Stdio coordinator integration tests.

tests/ceremony\_22\_of\_33.rs

Core 22-of-33 ceremony coverage.

Parameters

Parameters

The repository uses ML-DSA-65 / Dilithium3-style dimensions plus Luvion-specific threshold parameters.

Parameter

Parameter

Value

Value

Meaning

Meaning

N\_PARTIES

33

Total signing nodes.

THRESHOLD

22

Minimum nodes required for one signature attempt.

N

256

Polynomial degree.

Q

8,380,417

Ring modulus.

K

6

Public matrix rows.

L

5

Public matrix columns.

ETA

4

Secret coefficient bound.

GAMMA1

524,288

Mask bound base.

GAMMA2

261,888

Low/high bits decomposition bound.

TAU

49

Challenge polynomial weight.

BETA

196

TAU \* ETA

.

OMEGA

55

Maximum hint weight.

D

13

Public-key dropped bits.

Y\_BOUND\_PER\_NODE

23813

Per-node mask bound for threshold aggregation.

Parameter

Parameter

Value

Value

Meaning

Meaning

The per-node mask bound is chosen so the aggregate response can satisfy the ML-DSA norm requirement:

$$\text{THRESHOLD} * Y\_BOUND\_PER\_NODE + \text{TAU} * \text{ETA} < \text{GAMMA1} - \text{BETA}$$

Key Material Model

Key Material Model

The signing key is represented as ML-DSA material split across nodes.

The synthetic dealer in

gen\_shares

derives:

1

.

pk\_seed

.

2

.

Full secret vector

s1

.

3

.

Full secret vector

s2

.

4

.

Public matrix

$$A = \text{ExpandA}(\text{pk\_seed})$$

.

5

.

Public value:

$$t = A * s1 + s2$$

6

.

Power2Round decomposition:

(t1, t0) = Power2Round(t)

7

.

Public key:

pk = (pk\_seed, t1)

8

.

Shamir shares for each node:

s1\_i = ShamirShare(s1, i)

s2\_i = ShamirShare(s2, i)

t0\_i = ShamirShare(t0, i)

Each node receives one

NodeShare

containing:

index

dealer\_fingerprint

flags

s1 share

s2 share

t0 share

The share files are marked with

SHARE\_FLAG\_SYNTHETIC\_DEALER

. That flag is a clear signal that the material came from the synthetic dealer and is not production key material.

On-Disk Formats

On-Disk Formats

Public key files use:

magic: LVPK

version: 1

seed: 32 bytes

t1: K \* N \* 4 bytes

Node share files use:

magic: LVNS

version: 1

index: u64

dealer\_fingerprint: u64

flags: u8

s1: PolyVecL

s2: PolyVecK  
t0: PolyVecK

When a node starts, it loads

pk.bin

and its own

node<N>.bin

, verifies that the node id matches the share index, and verifies that the share dealer fingerprint matches the public key.

Network Runtime

Network Runtime

The networked signing path has two roles:

Role

Role

Binary

Binary

Responsibility

Responsibility

Signer node

node

Holds one share, listens on TCP, responds to protocol frames.

Coordinator

cluster\_sign

Connects to nodes, chooses 22 nodes, runs the signing attempt, aggregates, verifies.

The node process can run over stdio or TCP. The persistent cluster path uses TCP.

The coordinator supports:

Endpoint discovery from

--base-port

or explicit

--endpoints

.

Parallel or sequential probing.

Committee strategies:

first-alive-22

,

lowest-rtt-22

, and

random

.

t0

fetch modes:

on-demand

and

prefetch

.

Reconnect handling for transient transport failures.

JSON timing logs for each attempt and the full run.

Wire Protocol

Wire Protocol

The wire layer is versioned and length-prefixed.

Frame structure:

u32 length

u8 wire\_version

u8 msg\_kind

... bincode body

Frame constraints:

Field

Field

Constraint

Constraint

WIRE\_VERSION

Must match the local version.

MAX\_FRAME\_LEN

1 << 20

bytes.

msg\_kind

Must be one of the known protocol message

kinds.

Message kinds:

Kind

Kind

Direction

Direction

Purpose

Purpose

Ping

Coordinator -> node

Liveness probe.

Pong

Node -> coordinator

Node id and binary version.

Round1Request

Coordinator -> node

Ask node to sample mask and  
commit.

Round1Response

Node -> coordinator

Return

$W_i$

and commitment hash.

Round2Request

Coordinator -> node

Send challenge and participant set.

Round2Response

Node -> coordinator

Return partial

$z_i$

and

$cs2_i$

.

GetT0Request

Coordinator -> node

Fetch the node's

$t0$

share.

GetT0Response

Node -> coordinator

Return

$t0_i$

.

Error

Node -> coordinator

Protocol-level error response.

Shutdown

Coordinator -> node

Shutdown control message.

Kind

Kind

Direction

Direction

Purpose

Purpose

Signing Protocol

Signing Protocol

Committee Selection

Committee Selection

cluster\_sign

first probes all configured endpoints and keeps live connections. If fewer than 22 nodes are alive, it exits with the quorum failure code.

After probing, it selects exactly 22 nodes using the configured strategy:

first-alive-22

: lowest sorted live node ids.

lowest-rtt-22

: lowest measured probe RTT, tie-broken by node id.

random

: random 22 from the live set.

The selected participant list is sorted and must contain unique ids.

Attempt Setup

Attempt Setup

For each signing attempt, the coordinator creates:

request\_id: 32 random bytes

seed\_i: 64 random/domain-separated bytes per participant

nonce\_i: 32 random/domain-separated bytes per participant

The

request\_id

binds round 1 and round 2 on each node. Nodes cache round-1 mask state by

request\_id

and consume it exactly once during round 2.

Round 1: Commitment

Round 1: Commitment

For participant

i

, the node:

1

.

Validates the

request\_id

is not already active in its cache.

2

.

Samples a fresh masking vector:

$y_i \leftarrow$  bounded sample with  $|\text{coeff}| < Y\_BOUND\_PER\_NODE$

3

.

Computes:

$W_i = A * y_i$

4

.

Computes a commitment hash:

$\text{commit}_i = H(\text{"luvion\_round1\_commit\_v1"}, i, \text{nonce}_i, W_i)$

5

.

Stores

$y_i$

,

$\text{nonce}_i$

, and

$\text{commit}_i$

in the node cache under

request\_id

.

6

.

Returns

$W_i$

and

$\text{commit}_i$

.

Round1Output

redacts

$y_i$

from debug output and zeroes

$y_i$

on drop.

Challenge

Challenge

The coordinator aggregates:

$W = \text{sum}(W_i)$

Then it computes:

$W1 = \text{HighBits}(W)$

$\mu = \text{SHAKE256}(\text{"luvion\_challenge\_mu\_v1"}, \text{pk.seed}, \text{pk.t1})$

$\text{seed} = \text{SHAKE256}(\text{"luvion\_challenge\_seed\_v1"}, \mu, W1, \text{message})$

$c = \text{poly\_challenge}(\text{seed})$

$c$

is the sparse challenge polynomial with ML-DSA challenge weight.

Round 2: Partial Response

Round 2: Partial Response

For participant

$i$

, the node:

1

.

Looks up and removes its cached

$y_i$

using

$\text{request\_id}$

.

2

.

Validates the participant set has at least 22 sorted unique entries and contains itself.

3

.

Computes the Lagrange coefficient:

$\lambda_i = \text{LagrangeCoefficient}(i, \text{participants})$

4

.

Computes its partial response:

$z_i = y_i + \lambda_i * c * s1_i$

$cs2\_i = \lambda\_i * c * s2\_i$

5

.

Returns

$z\_i$

and

$cs2\_i$

.

Only the long-term secret shares are Lagrange-scaled. The fresh mask

$y\_i$

is not Lagrange-scaled; the aggregate mask is the direct sum of the per-node masks.

t0

t0

Fetch

Fetch

The aggregator also needs the threshold reconstruction of

t0

to compute the ML-DSA hint.

cluster\_sign

can fetch

t0

in two modes:

Mode

Mode

Behavior

Behavior

on-demand

Fetch

t0\_i

inside the attempt.

prefetch

Fetch

t0\_i

before attempts and reuse the

cache.

The optimized TCP path defaults to

prefetch

because it removes

GetT0

latency from the signing attempt itself.

Aggregation

Aggregation

The coordinator aggregates round-2 outputs:

$$z = \sum(z_i) = \sum(y_i) + c * s1$$

$$cs2 = \sum(cs2_i) = c * s2$$

It reconstructs

t0

from shares:

$$t0 = \sum(\lambda_i * t0_i)$$

$$ct0 = c * t0$$

Then it checks the ML-DSA rejection conditions:

$$\|z\|_{\infty} < \text{GAMMA1} - \text{BETA}$$

$$\|\text{LowBits}(W - cs2)\|_{\infty} < \text{GAMMA2} - \text{BETA}$$

$$\|ct0\|_{\infty} < \text{GAMMA2}$$

$$\text{hint\_weight} \leq \text{OMEGA}$$

If any check fails, the attempt is classified as a probabilistic rejection. This is not a transport failure.

Why

Why

r0\_norm

r0\_norm

Rejections Are Expected

Rejections Are Expected

r0\_norm

is the infinity norm of the low bits in:

$$r0 = \text{LowBits}(W - c*s2)$$

The acceptance rule is:

$$r0\_norm < \text{GAMMA2} - \text{BETA}$$

With the current ML-DSA-65 parameter set, this means:

$$\text{GAMMA2} = 261888$$

$$\text{BETA} = 196$$

$$\text{limit} = 261692$$

This check exists to keep the final threshold signature distribution compatible with ML-DSA rejection sampling. If a candidate attempt has

r0\_norm

above the limit,

the coordinator discards that attempt and retries with fresh per-node randomness. This protects against

secret-dependent leakage and ensures the verifier can recover the correct high bits from the final hint.

An

`r0_norm`

rejection means the network path and 22-node ceremony completed, but the sampled candidate did not pass the ML-DSA acceptance bounds. It is normal for some attempts to be rejected before a later attempt returns

`verified_signature`

. It only becomes a failed signing run if every attempt is rejected until

-

`-max-attempts`

is exhausted, which returns exit

4

.

If all checks pass, the final signature is:

`signature = (c, z, hint)`

where:

`hint = MakeHint(-ct0, W - cs2 + ct0)`

Verification

Verification

Verification checks:

1

.

`||z||_inf < GAMMA1 - BETA`

.

2

.

`hint_weight <= OMEGA`

.

3

.

Recompute:

`Az = A * z`

`ct1 = c * (t1 << D)`

`W' = Az - ct1`

`W1' = UseHint(W', hint)`

`c' = Challenge(pk, W1', message)`

4

Accept only if:

$c' == c$

cluster\_sign

verifies every successfully aggregated signature before returning success.

Attempt Outcomes and Exit Codes

Attempt Outcomes and Exit Codes

cluster\_sign

distinguishes protocol rejection from transport failure.

Exit

Exit

Code

Code

Meaning

Meaning

0

Verified signature produced.

3

Fewer than 22 alive nodes.

4

Max attempts exhausted due to probabilistic rejection.

5

Transport failure after retry budget.

1

CLI, configuration, decode, key loading, or internal error.

Exit

Exit

Code

Code

Meaning

Meaning

For this repository, exit

4

means the selected 22 nodes completed full ceremony attempts without transport failure, but no candidate signature passed the ML-DSA

rejection checks within the configured attempt budget. Demo scripts use a larger attempt budget and require exit

0

.

The most common retry reason in WAN demos is usually

reject\_reason=r0\_norm

. That status is expected protocol behavior, not a node failure. A successful run

may still contain earlier rejected attempts, as long as a later attempt returns

classification=verified\_signature

and exit

0

.

Node State and Replay Protection

Node State and Replay Protection

Each node has a

YntCache

keyed by

request\_id

.

The cache stores:

y\_i

nonce\_i

commitment\_hash

created\_at

Properties:

Round 1 rejects duplicate active

request\_id

s.

Round 2 consumes and removes the cached entry.

Unknown or expired

request\_id

s are rejected.

Cache entries expire by TTL.

Cache size is bounded.

Secret mask

y\_i

is zeroized when dropped.

This prevents a coordinator from reusing a node's one-time mask across different challenges.

Transport Robustness

Transport Robustness

The TCP path includes:

Per-connection read and write timeouts.

Parallel probing with probe RTT measurement.

Validation that probed node id matches the expected node id.

Version validation on wire frames.

Persistent committee connections reused across attempts.

Reconnect logic on transport errors.

JSON logs for attempts and run summaries.

The node TCP listener accepts concurrent connections so one idle client cannot block the signer process

from serving valid coordinators.

Performance Characteristics

Performance Characteristics

The measured optimized local path is approximately:

Metric

Metric

Local Persistent

Local Persistent

Cluster

Cluster

Probe

36ms

t0

prefetch

41ms

Ceremony attempt

130ms

Wall time

233ms

Reconnects

0

Transport failures

0

The measured optimized DigitalOcean 25-droplet path is approximately:

Metric

Metric

DigitalOcean Spread-25

DigitalOcean Spread-25

Probe

260ms

t0

prefetch

195ms

Ceremony attempt

475ms

Full

cluster\_sign

invocation

1.128s

Reconnects

0

Transport failures

0

Metric

Metric

DigitalOcean Spread-25

DigitalOcean Spread-25

The main latency contributors in WAN mode are network probe RTTs,

t0

prefetch, and cross-region round-trip time during round 1 and round 2.

Current Limitations

Current Limitations

The repository currently uses a synthetic dealer for easy testing. Production deployment requires a real DKG or secure key-generation ceremony.

The signing math uses schoolbook polynomial multiplication in correctness-critical signing paths.

Comments in the code note an unresolved NTT/Montgomery-convention issue, so the NTT fast path is not used for those operations.

Very small attempt budgets can still produce exit

4

because ML-DSA rejection sampling may reject candidate attempts. Use the demo defaults or increase --max-

attempts

when a verified signature is mandatory.

The current demo and test deployment model exposes raw TCP node ports. A production system should add authenticated transport, access control, key management, observability, and stronger operator controls.

Validation Coverage

## Validation Coverage

Important validation paths include:

Command

Command

Coverage

Coverage

cargo check

Type and compile validation.

`cargo test --test ceremony_22_of_33`

Core threshold ceremony behavior.

`cargo test --test coordinator_integration`

Stdio coordinator integration.

`cargo test --test cluster_sign_tcp -- --test-threads=1`

Persistent TCP cluster behavior, retries, timeout handling, idle connection handling, probe timeout behavior.

`cargo build --release --bin gen_shares --bin node -  
-bin cluster_sign`

Release binaries used by local and real-world runs.

Recent validation confirmed:

TCP idle connections do not block signer nodes.

Probe ping uses the configured I/O timeout.

Wire frame version mismatches are rejected.

The persistent local 33-node flow can run a 22-node sign with zero reconnects and zero transport failures.

The DigitalOcean 25-droplet flow can deploy 33 nodes, sign with 22 endpoints, and clean up all droplets.